

# Cambridge International AS & A Level

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NAME

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## MATHEMATICS

9709/12

Paper 1 Pure Mathematics 1

October/November 2024

**1 hour 50 minutes**

You must answer on the question paper.

You will need: List of formulae (MF19)

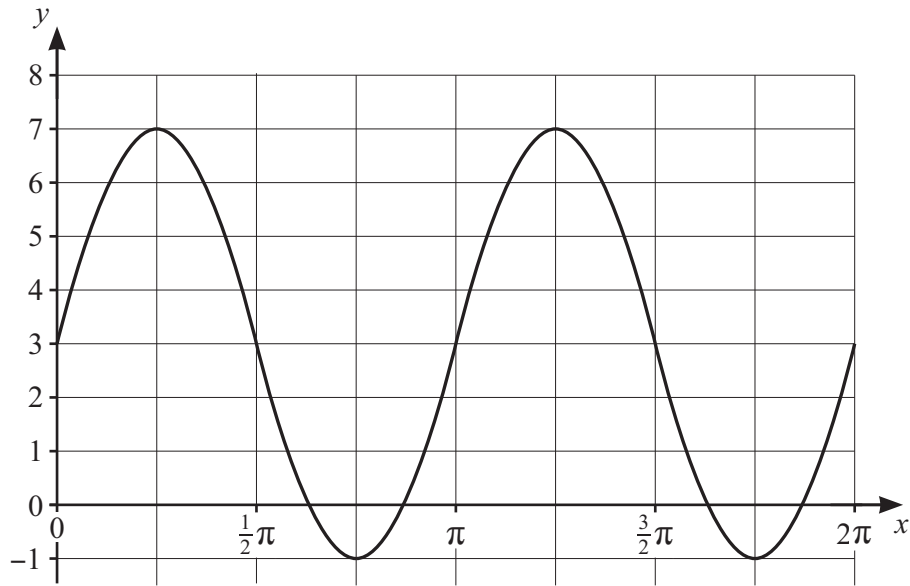
## INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

## INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [ ].

1



The diagram shows the curve with equation  $y = a \sin(bx) + c$  for  $0 \leq x \leq 2\pi$ , where  $a$ ,  $b$  and  $c$  are positive constants.

- (a) State the values of  $a$ ,  $b$  and  $c$ . [3]

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- (b) For these values of  $a$ ,  $b$  and  $c$ , determine the number of solutions in the interval  $0 \leq x \leq 2\pi$  for each of the following equations:

(i)  $a \sin(bx) + c = 7 - x$  [1]

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(ii)  $a \sin(bx) + c = 2\pi(x - 1)$ . [1]

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- 2 The first term of an arithmetic progression is  $-20$  and the common difference is  $5$ .

(a) Find the sum of the first 20 terms of the progression.

[2]

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It is given that the sum of the first  $2k$  terms is 10 times the sum of the first  $k$  terms.

(b) Find the value of  $k$ .

[3]

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- (a)** Find and simplify an expression for the gradient of the chord  $AB$  in terms of  $h$ . [3]

[illegible]

- [illegible]

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5 The function  $f$  is defined by  $f(x) = \frac{2x+1}{2x-1}$  for  $x < \frac{1}{2}$ .

(a) (i) State the value of  $f(-1)$ .

[1]

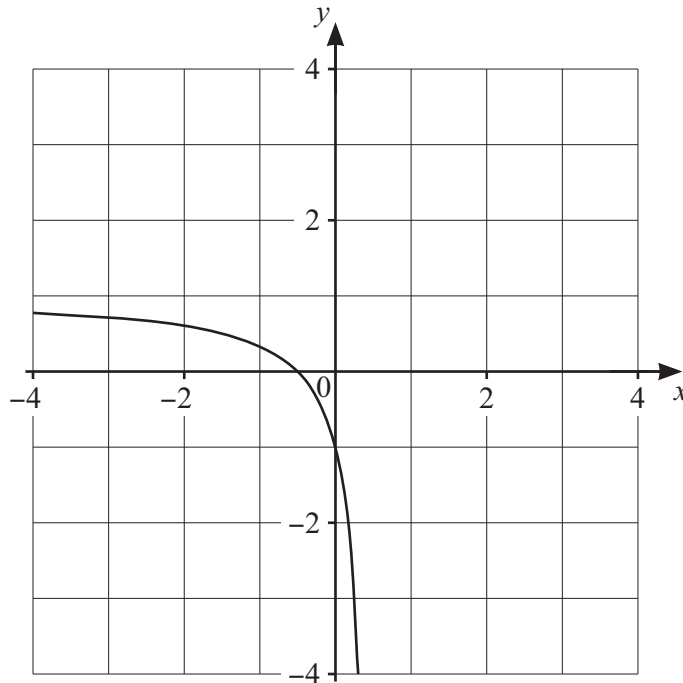
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(ii)



The diagram shows the graph of  $y = f(x)$ . Sketch the graph of  $y = f^{-1}(x)$  on this diagram. Show any relevant mirror line. [2]

(iii) Find an expression for  $f^{-1}(x)$  and state the domain of the function  $f^{-1}$ . [4]

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The function  $g$  is defined by  $g(x) = 3x + 2$  for  $x \in \mathbb{R}$ .

- (b) Solve the equation  $f(x) = gf\left(\frac{1}{4}\right)$ . [3]

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It is given that the perimeter of the plate is 14 cm and the area of the plate is  $10\text{ cm}^2$ .

Given that  $r > \frac{3}{2}$  and  $\theta < \frac{3}{4}$ , find the values of  $r$  and  $\theta$ . [6]

[illegible]



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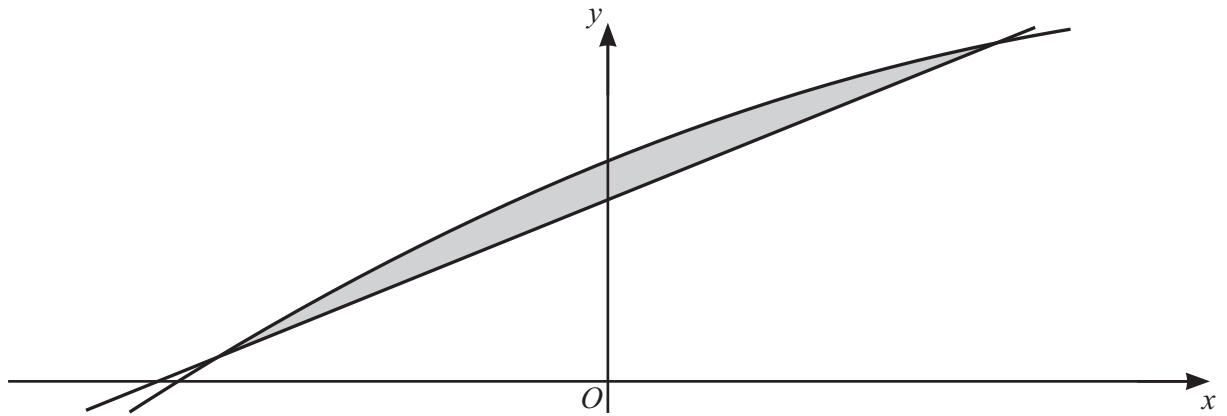
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Handwriting practice area with 20 horizontal dotted lines.

- 7 (a) By expressing  $-2x^2 + 8x + 11$  in the form  $-a(x-b)^2 + c$ , where  $a$ ,  $b$  and  $c$  are positive integers, find the coordinates of the vertex of the graph with equation  $y = -2x^2 + 8x + 11$ . [3]

(b)



The diagram shows part of the curve with equation  $y = -2x^2 + 8x + 11$  and the line with equation  $y = 8x + 9$ .

Find the area of the shaded region.

Handwriting practice area with 20 sets of horizontal dotted lines.

(a) Express the equation in the form  $(x-a)^2 + (y-b)^2 = r^2$ , where  $a$  is to be given in terms of  $p$  and  $r^2$  is to be given in terms of  $p$  and  $q$ . [2]

[illegible]

**(b) (i)** Find the equation of the normal to the circle at the point  $A$ . [3]

This image shows a full page of white paper with horizontal dashed lines, typical of primary school handwriting practice paper. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

[5]

[illegible]

- (a)** It is given that one of the points of intersection of the curve and the line has coordinates  $\left(\frac{5}{2}, \frac{1}{2}\right)$ .

[illegible]

- (b) It is given instead that the line and the curve do **not** intersect.

Find the set of possible values of  $p$ .

[3]

- (a) Find the equation of the normal to the curve at the point  $(1, 0)$ . [3]

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